



Life Cycle Assessment
A product-oriented method
for sustainability analysis

UNEP LCA Training Kit
Module k – Uncertainty in LCA



UNEP

Life Cycle



Initiative



Contents

This module requires the delegate to have basic understanding of statistics and matrix algebra.

- Introduction to uncertainties
- Treatment of uncertainties
- Elements in uncertainty handling
- Sensitivity of LCA results
- Using statistics in LCA

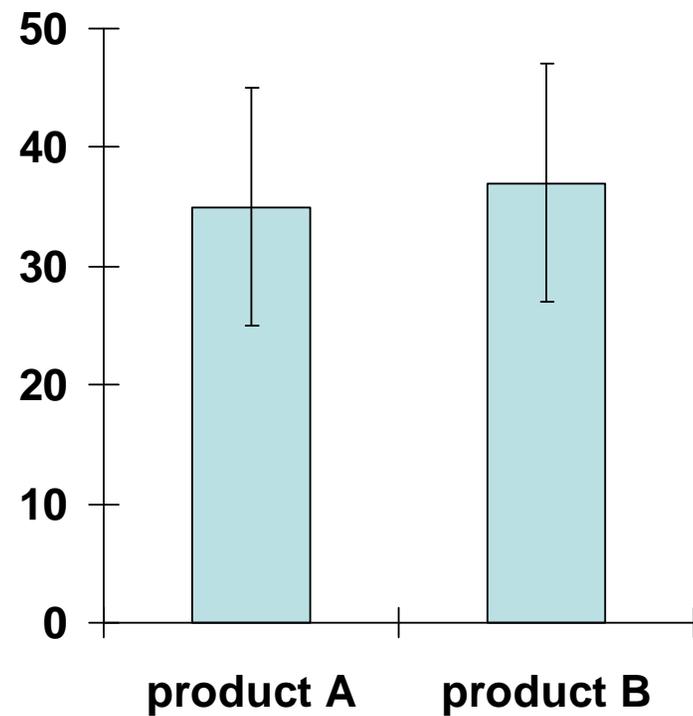
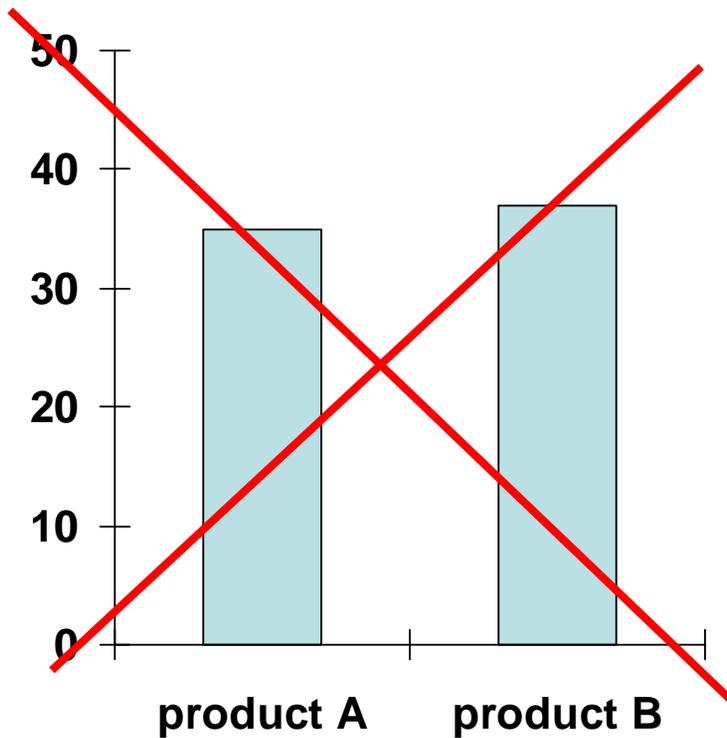
Introduction to uncertainties

- **Uncertainty in LCA is increasingly recognized as being important:**
 - uncertainties in data
 - uncertainties due to methodological choices
 - processing of uncertainties
 - decision-making under uncertainty

How to manage uncertainties?

- **Conduct more research**
 - that's in every "recommendation for future research"
- **Abandon LCA**
 - not advisable
- **Interpret LCA results cautiously**
 - of course, but how?
- **Involve stakeholders**
 - does this reduce or increase the uncertainty?
- **Rerun the LCA with different data and choices**
 - sounds unsystematic
- **Use Monte Carlo analyses**
 - How to?
- **Use analytical approaches towards uncertainty**
 - How to?

Presenting uncertainties

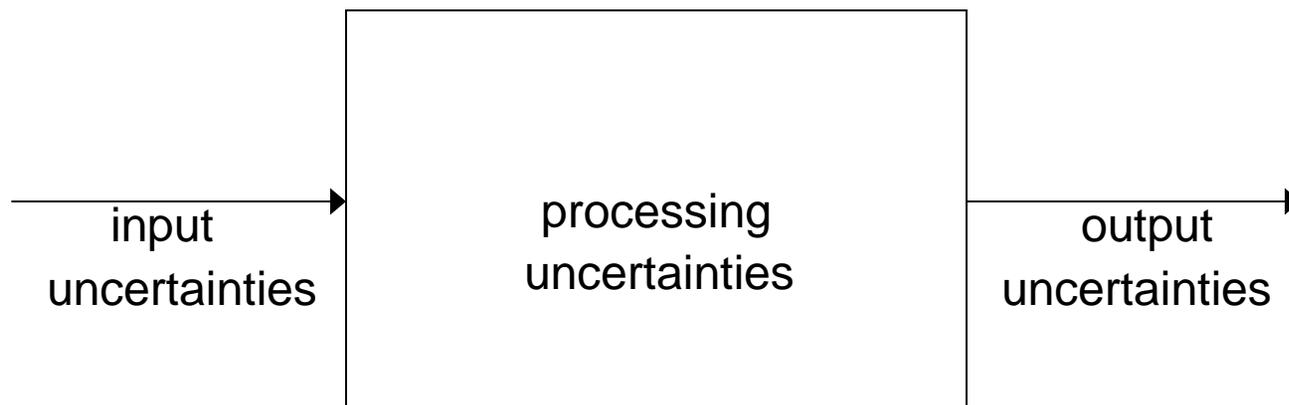


Treatment of uncertainties

- **Four main paradigms:**
 - 1. **“scientific”** approach (more research, better data)
 - 2. **“social”** (constructivist) approach (stakeholders, agreements)
 - 3. **“legal”** approach (authoritative bodies)
 - 4. **“statistical”** approach (Monte Carlo, confidence intervals)
- **What makes paradigm 4 special?**
 - 1, 2, 3 reduce uncertainty
 - 4 incorporates uncertainty

Treatment of uncertainties

- **General modeling framework**



Treatment of uncertainties

- **Processing uncertainties:**
 - parameter variation/scenario analysis
 - sampling methods (Monte Carlo)
 - analytical methods
 - non-traditional methods (fuzzy set, Bayesian)

Treatment of uncertainties

- **Input uncertainties:**
 - several values/choices
 - distributions
 - variances
 - data quality indicators (DQIs)

Treatment of uncertainties

- **Output uncertainties:**
 - results for different options
 - histograms
 - confidence intervals

Elements in uncertainty handling

- **Standardization**
 - **terminology**
(example: what is the difference between sensitivity and uncertainty analysis)
 - **symbols**
(example: what do we mean with μ ?)
 - **data format**
(example: how to report a lognormal distribution?)

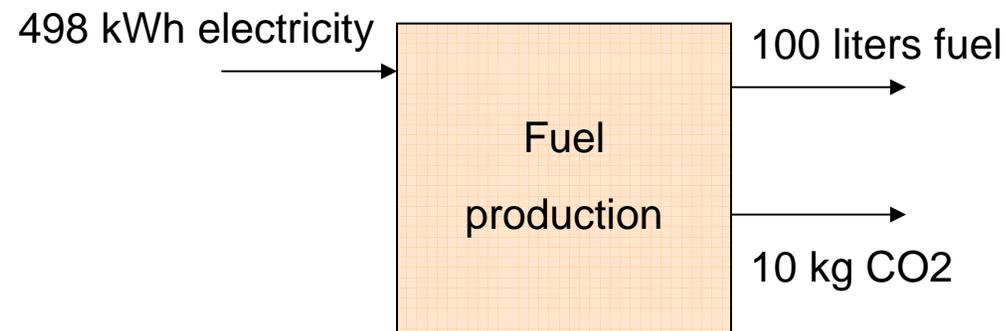
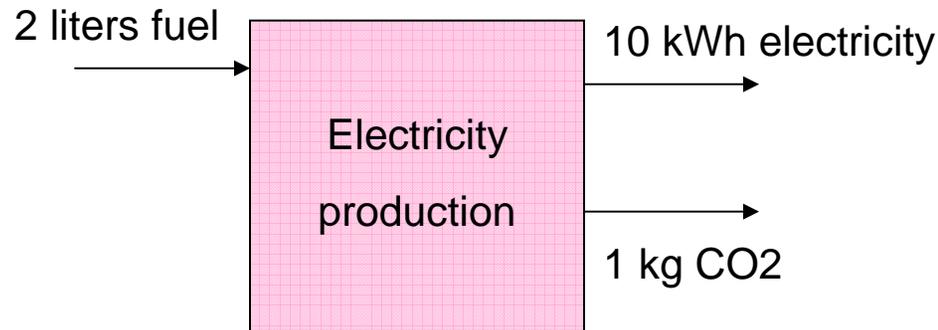
Elements in uncertainty handling

- **Education**
 - **concepts**
(what is a significant difference?)
 - **reporting**
(how many digits?)
 - **value of not reducing but incorporating uncertainty**

Elements in uncertainty handling

- **Development**
 - **approaches**
(Monte Carlo, bootstrapping, principal components analysis, condition number, etc.)
 - **software**
(many approaches)
 - **databases**
(that support many approaches)
 - **guidelines**
(for applying which approach in which situation)

Sensitivity of LCA results

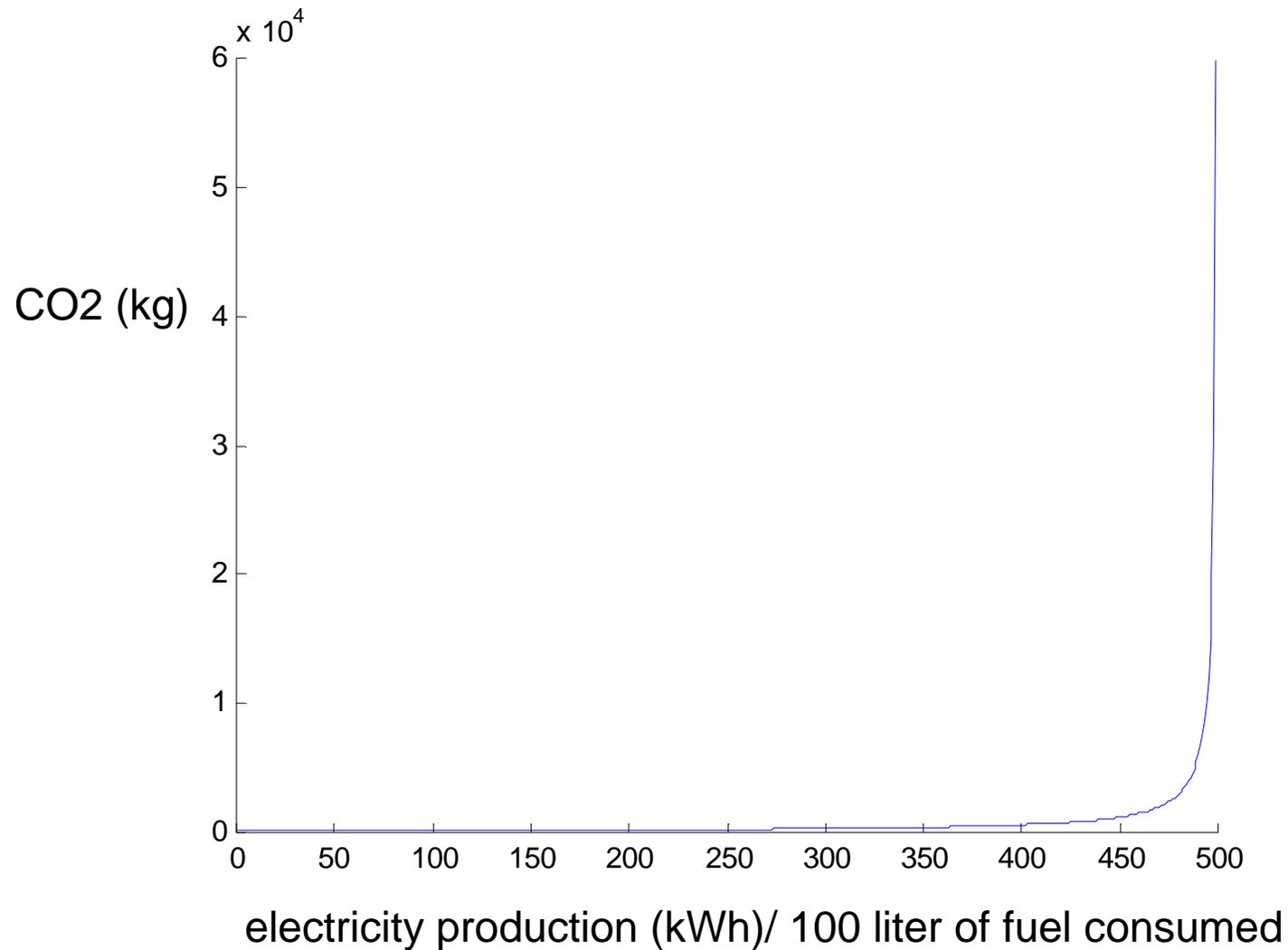


- Reference flow: 1000 kWh electricity
- Inventory result: 30,000 kg CO₂

Sensitivity of LCA results

- Change “498” into “499” (i.e. 0.2% change)
- “30.000” is changed into “60.000” (i.e. 100% change)
- Magnification of uncertainty by a factor 500 is possible in a system that is
 - small
 - Linear
- Can we understand this?

Sensitivity of LCA results



Sensitivity of LCA results

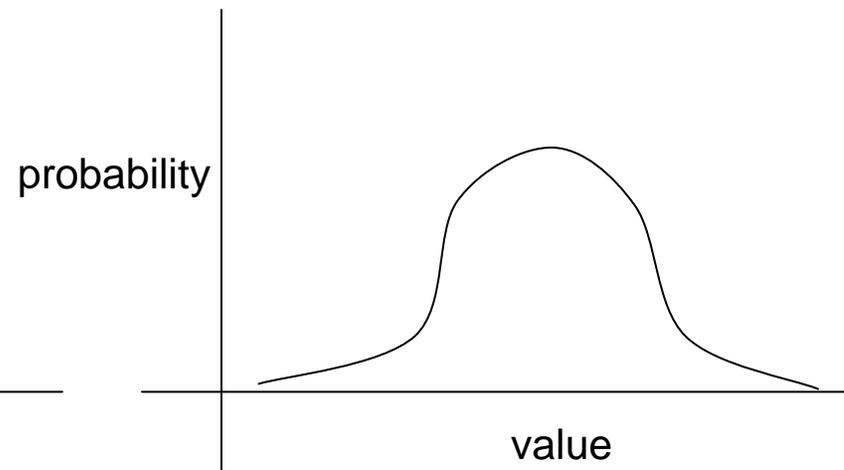
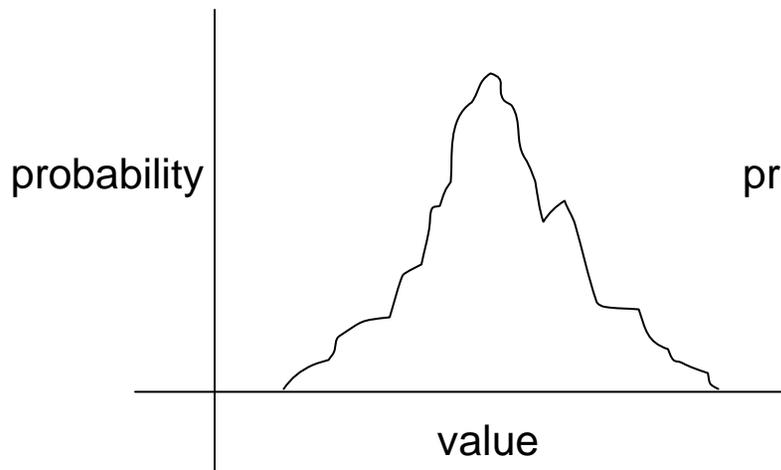
- **Sometimes, a small change of a parameter can induce a large change.**
 - of which the magnification factor $\gg 1$
 - or $\ll -1$
- **A parameter is sensitive only in a certain range.**
 - only for a certain reference flow

Sensitivity of LCA results

- Precise knowledge of these parameters is critical for the outcome of the LCA.
- Changing these parameters by new design, new technology, etc. significantly influences the environmental performance.
- These sensitive parameters are important for computational stability.

Using statistics in LCA

- **Probability distribution**
 - Full empirical distribution
 - Textbook normal distribution often assumes mean $\mu=12$ and deviation $\sigma=3$
 - Unspecified distribution can note parameters such as mean, standard deviation, and bias, ...



Using statistics in LCA

- **Distribution**
 - population versus sample
- **Parameter**
 - population (“true value”) versus sample (“estimated value”)
- **Confidence interval**
 - interval in which the true value is expected to be found with a predefined certainty (e.g., 95%)
 - This is often approximately 4 standard deviations wide.

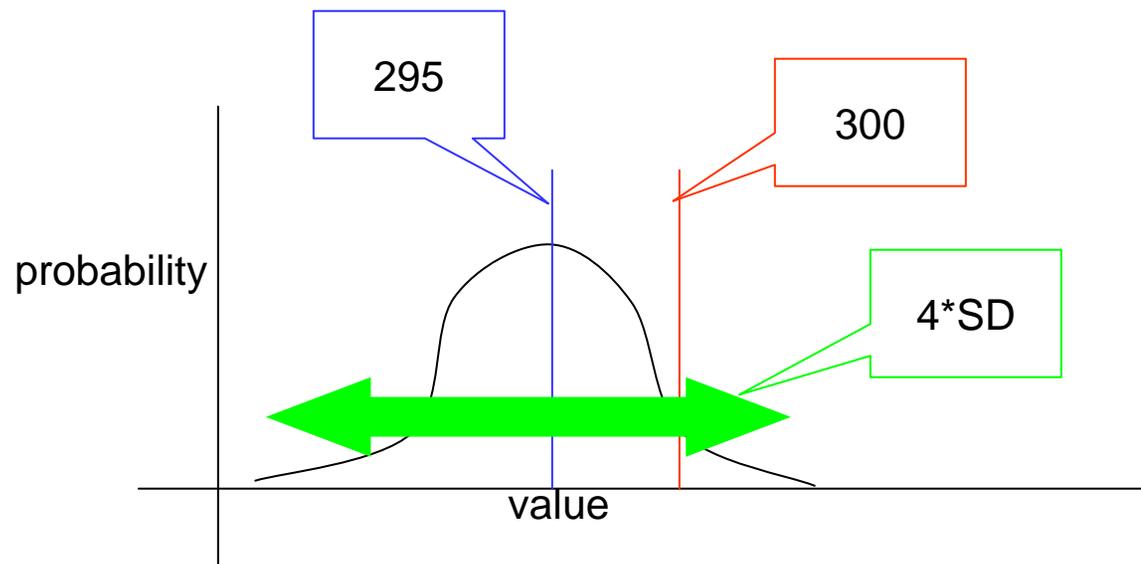
Using statistics in LCA

- **Statistical test**
 - analysis that combines statistical theory and empirical data
 - to test whether a predefined null-hypothesis can be rejected at a predefined significance level
- **Null-hypothesis**
 - translation of a question into an explicit statement that can be submitted to statistical testing
 - stand-alone, e.g. “CO₂ -emission = 300 kg”
 - comparative, e.g. “CO₂ -emission of product A and B is equal”

Using statistics in LCA

- **Decision**

- determine the probability of the null-hypothesis
- e.g., if CO₂ -emission = 295 kg with a standard deviation of 1 the null-hypothesis will be rejected
- or, if CO₂ -emission = 295 kg with a standard deviation of 3 it will not be rejected (but not accepted!)



Using statistics in LCA

- **Significance**
 - if the null-hypothesis is rejected at the specified significance level, there is a significant difference/effect/etc.
 - For instance, if “CO₂-emission = 300 kg” is rejected, the CO₂ -emission is significantly different from 300 kg
 - or, if “CO₂ -emission of product A and B is equal” is rejected, there is a significant difference between the CO₂-emission of these products
- **Significant versus large**
 - a significant difference may be small or large
 - a large difference may be insignificant or significant

Using statistics in LCA

- **Numerical treatment**
 - parametric variation, e.g., scenarios (not very systematic)
 - sampling methods, e.g., Monte Carlo analysis
- **Analytical treatment**
 - based on formulas for error propagation

Monte Carlo analysis in 5 steps

- 1. Consider every input parameter as a stochastic variable with a specified probability distribution**
 - For instance, CO₂-emission of electricity production follows a normal distribution with a mean of 1 kg and a standard deviation of 0.05 kg
- 2. Construct the LCA-model with one particular realization of every stochastic parameter**
 - For instance, CO₂-emission of electricity production is 0.93 kg

Monte Carlo analysis in 5 steps

- 3. Calculate the LCA-results with this particular realization**
 - e.g., CO₂-emission of system is 28,636 kg
- 4. Repeat this for a large number of realisations**
 - e.g., number of runs $N = 1000$
- 5. Investigate statistical properties of the sample of LCA-results**
 - e.g., the mean, the standard deviation, the confidence interval, the distribution

Using statistics in LCA

- **Analytical treatment in 2 steps**
 1. **Consider every input parameter as a stochastic variable with a specified mean and standard deviation (or variance)**
 - For instance, CO₂-emission of electricity production has a mean of 1 kg and a standard deviation of 0.05 kg
 2. **Apply classical rules of error propagation**
 - For instance, elaborate formula for standard deviation (or variance) of CO₂-emission of system

Using statistics in LCA

- Example: area of sheet of paper

$$A = l \times h$$

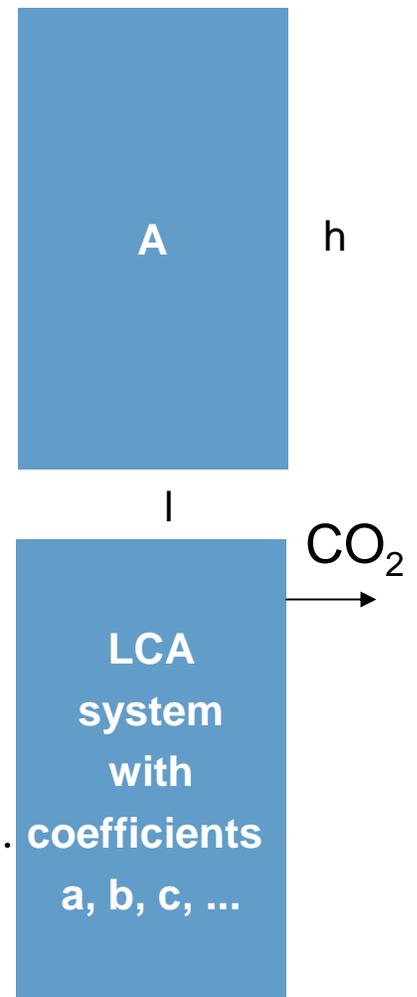
$$\text{var}(A) = \left(\frac{\partial A}{\partial l}\right)^2 \text{var}(l) + \left(\frac{\partial A}{\partial h}\right)^2 \text{var}(h)$$

$$\text{var}(A) = h \times \text{var}(l) + l \times \text{var}(h)$$

- Same idea for LCA:

$$\text{CO}_2 = f(a, b, c, \dots)$$

$$\text{var}(\text{CO}_2) = \left(\frac{\partial f}{\partial a}\right)^2 \text{var}(a) + \left(\frac{\partial f}{\partial b}\right)^2 \text{var}(b) + \left(\frac{\partial f}{\partial c}\right)^2 \text{var}(c) + \dots$$



Using statistics in LCA

- **Numerical**
 - is simple to understand
 - does not require explicit formulas
 - can deal with model choices as well
- **Analytical**
 - is fast
 - does not require runs
 - does not require probability distributions
 - enables a decomposition into key issues

Using statistics in LCA

- **LCA requires explicit formulas.**

- for LCIA widely published

$$h_j = \sum_i Q_{ji} g_i \quad \text{or} \quad \mathbf{h} = \mathbf{Qg}$$

- but for LCI?

$$g_i = ? \quad \text{or} \quad \mathbf{g} = ?$$

- **The answer can be found in matrix algebra.**



You may want to review some of these approaches to dealing with uncertainty in LCA.

- **Introduction to uncertainties**
- **Treatment of uncertainties**
- **Elements in uncertainty handling**
- **Sensitivity of LCA results**
- **Using statistics in LCA**



Module contents

The last module addresses carbon footprinting.

I	Carbon footprint
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